# Amplitude- and Phase-Resolved Nanospectral Imaging of Phonon Polaritons in Hexagonal Boron Nitride 

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#### Abstract

Phonon polaritons are quasiparticles resulting from strong coupling of photons with optical phonons. Excitation and control of these quasiparticles in 2D materials offer the opportunity to confine and transport light at the nanoscale. Here, we image the phonon polariton (PhP) spectral response in thin hexagonal boron nitride (hBN) crystals as a representative 2 D material using amplitude- and phase-resolved scattering scanning near-field optical micros-  copy ( $s$-SNOM) using broadband mid-IR synchrotron radiation. The large spectral bandwidth enables the simultaneous measurement of both out-of-plane ( $780 \mathrm{~cm}^{-1}$ ) and in-plane $\left(1370 \mathrm{~cm}^{-1}\right) \mathrm{hBN}$ phonon modes. In contrast to the strong in-plane mode, the out-of-plane PhP mode response is weak. Measurements of the PhP wavelength reveal a proportional dependence on sample thickness for thin hBN flakes, which can be understood by a general model describing two-dimensional polariton excitation in ultrathin materials.


KEYWORDS: phonon polariton, boron nitride, near-field spectroscopy, synchrotron infrared nanospectroscopy (SINS)

Phonon polaritons ${ }^{1}$ (PhPs) result from coupling of photons with optical phonons in polar crystals. Unlike plasmon polaritons, ${ }^{2-4}$ which usually span a very broad energy range, PhPs provide a spectrally selective response related to the optical phonon modes in the infrared to terahertz spectral range. The PhPs can have strong spatial confinement and may enable potential applications for enhanced IR light-matter interaction, ${ }^{5,6}$ high-density IR data storage, ${ }^{7}$ coherent thermal emission, ${ }^{8}$ development of metamaterials, ${ }^{9,10}$ and frequencytunable terahertz wave generation. ${ }^{11}$

Hexagonal boron nitride ( hBN ) is a convenient model system for studying PhPs in ultrathin materials because hBN flakes with different thicknesses are easy to prepare with high quality and no dangling bonds as a two-dimensional (2D) van der Waals material. It has two Reststrahlen bands in the midinfrared region spanning the transverse ( $\omega_{\text {TO }}$ ) and longitudinal $\left(\omega_{\mathrm{LO}}\right)$ phonon frequencies of the out-of-plane mode ( $\omega_{\mathrm{TO}}=$ $760, \omega_{\mathrm{LO}}=825 \mathrm{~cm}^{-1}$ ) and the in-plane mode ( $\omega_{\mathrm{TO}}=1370$, $\omega_{\mathrm{LO}}=1614 \mathrm{~cm}^{-1}$ ). Both the lower frequency out-of-plane mode and the higher frequency in-plane mode have negative real parts of the dielectric function and thus have the potential to support PhPs. ${ }^{12}$ Furthermore, hBN is a promising material for nanotechnology applications due to its 2D layered structure, excellent electrical insulation, and chemical and thermal
stability. It has attracted great interest as a substrate for highmobility graphene, ${ }^{13-17}$ as an ideal dielectric layer and spacer for 2D heterostructures, ${ }^{18,19}$ and for its intrinsic UV lasing response. ${ }^{20}$

Recently, the hBN PhP related behavior started to attract much interest. ${ }^{21-24}$ Dai et al. studied PhPs in thin hBN flakes with laser-based scattering scanning near-field optical microscopy ( $s$-SNOM) and observed a thickness-dependent PhP dispersion ${ }^{21}$ in the upper spectral range around the in-plane ( $\sim 1370 \mathrm{~cm}^{-1}$ ) vibration phonon mode. However, they reported only spectral amplitude information on the coherent PhP response at the higher frequency in-plane phonon mode and relied on complex modeling to explain the thicknessdependent PhP dispersion. Here, we use broadband synchrotron infrared nanospectroscopy (SINS; see Methods) ${ }^{25}$ for simultaneous amplitude and phase-resolved spatiospectral imaging of the PhPs in thin hBN flakes. We measure the PhP response for both the low-frequency out-of-plane ( $\sim 780$ $\mathrm{cm}^{-1}$ ) and high-frequency in-plane ( $\sim 1370 \mathrm{~cm}^{-1}$ ) characteristic phonon modes of hBN. We describe the observed standing wave PhP behavior using a simple cavity model to

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Figure 1. (A) Schematic of synchrotron infrared nanospectroscopy (SINS) using coherent broadband synchrotron infrared radiation provided by the Advanced Light Source (ALS) as the synchrotron source, a KBr beamsplitter (BS), and an atomic force microscope (AFM). (B) The synchrotron IR light illuminates the conductive AFM tip, which launches polariton waves that propagate radially outward from the tip along the $h B N$ surface and are reflected off the edges, forming standing waves with the tip. (C) Representative amplitude $|A(\bar{\nu})|$ spectra taken from three different positions (marked with colored dots) of a 75 nm thick hBN flake, shown in the inset. A peak appears on the high-frequency side of the main in-plane phonon peak near $1370 \mathrm{~cm}^{-1}$ in the spectra taken near the hBN edge, due to the interference of the forward-moving and backward-moving polariton wave reflected by the hBN edge.


Figure 2. Sequence of real-space SINS images of near-field (A) amplitude $|A(\bar{\nu})|$ and (B) phase $\Phi(\bar{\nu})$ near an edge of a 160 nm thick hBN flake acquired simultaneously. The bottom image in both $(A)$ and $(B)$ is the topography of the sample, showing the sample edge on the left side of the image stack at $x=0$ (indicated by the dotted green line). The color maps for the amplitude and phase images have been individually normalized to the maximum and minimum amplitude and phase value of each image for better visibility. Interference between the forward-propagating and backreflected polariton waves modulates the near-field amplitude and phase as a function of the distance from the hBN edge. Different interference patterns are due to different polariton wavelengths.
simultaneously fit the amplitude and phase, ${ }^{26}$ which allows us to extract the wavelength and reflection coefficients as they relate to the dispersion relation. We also develop a simple theory, general to 2 D polaritons ${ }^{27,28}$ in ultrathin layered materials, to describe the proportional dependence of the phonon polariton wavelength to sample thickness. ${ }^{21}$

Near-field Fourier transform infrared nanospectroscopy and imaging were performed with SINS at the Advanced Light Source. ${ }^{25}$ In brief, broadband synchrotron IR light is focused onto the apex of a metal-coated atomic force microscope (AFM) tip with apex radius $r<25 \mathrm{~nm}$ (Figure 1A). The resulting large near-field momentum provided by the spatial field localization at the apex extends into the typical momentum range of hBN phonon polaritons and allows for their optical excitation. The excited polariton wave propagates
radially outward from the near-apex launched region along the hBN surface (Figure 1B). When reaching the sample edge, the polariton waves are reflected. The back-reflected polariton waves interfere with the excitation field at the tip and modify the amplitude and the phase of the tip-scattered near-field, which is detected by interferometric heterodyne amplification. ${ }^{25}$ This allows for the spatial and spectral imaging of the PhP waves. The strong dependence of the PhP wavelength on excitation frequency leads to a variation in the observed spectra, as shown in Figure 1C with three representative amplitude spectra taken at different distances from the edge of a 75 nm thick hBN flake.

To prepare samples, $\mathrm{hBN}^{29}$ is directly exfoliated onto a $\mathrm{SiO}_{2} / \mathrm{Si}(300 \mathrm{~nm} / 500 \mu \mathrm{~m})$ substrate with adhesive tape. The achieved hBN flake thickness varies from several atomic layers
to hundreds of nanometers. After taking an AFM image of an hBN flake to determine its thickness, we either perform a single SINS line scan perpendicular to a straight edge or record full spatiospectral area scans in the edge region. Several specimens with thickness varying from 3 to 160 nm were measured and analyzed.

We measure both amplitude and phase of the BN phonon polariton near-field response. This provides for a consistency check given the inherent experimental uncertainty in $s$-SNOM measurements of phase and amplitude alone. In principle, amplitude and phase are Kramers-Kronig related. However, a unique phase assignment is difficult in general from an amplitude measurement alone (or vice versa) using the Kramers-Kronig relation, because the limited spectral range of the experiment does not allow for amplitude measurements over a broad enough frequency range for a unique spectral phase assignment. We therefore measure spectral amplitude and phase directly from the asymmetric near-field signal interferograms. ${ }^{25}$

Figure 2 A and B show the real-space 2 D mapping of the spectral near-field amplitude $|A(\bar{\nu})|$ and phase $\Phi(\bar{\nu})$ of a 160 nm thick hBN flake for selected excitation frequencies, respectively. The bottom images of Figure 2A and B are the topography of the sample; the straight edge is located on the left side $(x=0 \mu \mathrm{~m})$. Interference between the forwardpropagating and back-reflected polariton waves modulates the near-field amplitude and phase as a function of the distance from the hBN edge. Different interference patterns reflect different polariton wavelengths. All the interference patterns are parallel to the sample edge, showing uniform reflection of the PhP wave at the edge. Progressing from the top image to the bottom image, the maximum amplitude (Figure 2A) and minimum phase (Figure 2B) gradually move away from the hBN edge, due to the increase in polariton wavelength with decreasing incident IR frequency.

The large bandwidth of the synchrotron light enables us to simultaneously measure the near-field PhP IR response in a range that covers both the in-plane and out-of-plane phonon modes. Figure 3A and B show broadband spatiospectral maps of near-field amplitude and phase, respectively, for a line scan perpendicular to the edge of the sample. Increased scattering amplitudes (Figure 3A) around 1370 and $780 \mathrm{~cm}^{-1}$ correspond to the hBN in-plane and out-of-plane phonon modes, respectively, and the spectral feature around $1130 \mathrm{~cm}^{-1}$ is due to the $\mathrm{SiO}_{2}$ phonon of the substrate. ${ }^{25,27}$ Spatially dependent features arising from propagating polaritons show up between the transverse $\left(\omega_{\mathrm{TO}}\right)$ and longitudinal ( $\omega_{\mathrm{LO}}$ ) optical phonon frequencies in both the in-plane and out-ofplane phonon modes (Figure 3A and B). This phenomenon is revealed more clearly in Figure 3C and D with five spectra at the positions marked with dashed lines in Figure 3A and B, respectively. For the in-plane phonon mode, the main peak at $\sim 1370 \mathrm{~cm}^{-1}$ remains largely unchanged in Figure 3C, while the interference peak on the right shoulder of the main phonon peak moves progressively to lower frequency as the tip scans farther from the sample edge. Likewise, the main phonon peak of the out-of-plane phonon mode at $\sim 770 \mathrm{~cm}^{-1}$ remains largely unchanged, but in this case, the interference peak moves progressively to higher frequency as the tip scans farther from the sample edge. A similar PhP behavior is observed for both modes in the near-field phase spectra presented in Figure 3D.

To highlight these changes in PhP wavelength with excitation frequency, we show expanded views of the hBN in-plane and


Figure 3. Spatiospectral SINS line scan of hBN phonon polaritons with spectral cuts. Simultaneously acquired (A) near-field amplitude $|A(\bar{\nu})|$ and (B) phase $\Phi(\bar{\nu})$ linescan obtained perpendicular to the edge of a 147 nm thick hBN flake. The green arrow at $x=0$ marks the edge of the hBN crystal. Signals around 1370 and $780 \mathrm{~cm}^{-1}$ correspond to the in-plane and out-of-plane phonon mode in hBN , respectively, and the signal around $1130 \mathrm{~cm}^{-1}$ is related to the $\mathrm{SiO}_{2}$ phonon mode of the substrate. Strong PhP features only appear around the in-plane phonon mode ( $1370 \mathrm{~cm}^{-1}$ ). Near-field (C) amplitude and (D) phase spectra at five representative positions, marked in (A) and (B).
out-of-plane spectral regions in Figures 4 and 5, respectively, along with distance profiles at representative excitation frequencies. These distance profiles clearly show the interference between the forward and back-reflected PhP waves in both the amplitude and phase responses. For the in-plane mode, the PhP wavelength is longest at low frequencies and becomes progressively shorter as the excitation frequency approaches the $\omega_{\mathrm{LO}}=1614 \mathrm{~cm}^{-1}$ limit, whereas for the out-of-plane limit, the PhP wavelength is shortest at low frequencies and becomes progressively longer as the excitation frequency approaches the $\omega_{\mathrm{LO}}=825 \mathrm{~cm}^{-1}$ limit. This behavior is consistent with the fact that hBN is a natural hyperbolic material, whose in-plane and out-of-plane real part of dielectric functions are of opposite sign in a certain energy range related to its phonon modes. ${ }^{30}$ In hBN , the lower frequency out-of-plane mode is a type I hyperbolic mode with $\operatorname{Re}\left(\varepsilon_{\perp}\right)<0$ and $\operatorname{Re}\left(\varepsilon_{\|}\right)>0$, whereas the higher frequency in-plane mode is a type II hyperbolic mode with $\operatorname{Re}\left(\varepsilon_{\perp}\right)>0$ and $\operatorname{Re}\left(\varepsilon_{\|}\right)<0$. hBN thus has both types of hyperbolic response in the same sample. The two types of hyperbolic modes have different PhP wavelength dispersion relations with respect to the excitation frequency, with type I modes illustrating an ascending behavior, in which the polariton wavelength increases with excitation frequency, and type II


Figure 4. Cavity model analysis of experimental spatial and spectral profiles. Experimental (A) SINS amplitude $|A(\bar{\nu})|$ and (B) phase $\Phi(\bar{\nu})$ spatiospectral linescan in the region of the hBN in-plane phonon mode of the 147 nm thick hBN flake. Note the different color scales from Figure 3 with absolute phase values. Simulated SINS (C) amplitude and (D) phase spatiospectral linescan of the same hBN flake in (A) and (B) using the cavity model discussed in the text. (E) Experimental (blue) and simulated SINS amplitude (black) distance profiles extracted from (A) and (C), respectively. (F) Experimental (red) and simulated SINS phase (black) distance profiles extracted from (B) and (D), respectively.
modes exhibiting a descending behavior, with the wavelength decreasing with excitation frequency.

The distance profiles of the amplitude and phase measurements in Figure 4C and D show consistent patterns in which the maximum phase response occurs at the edge of the flake, whereas the maximum amplitude response is displaced from the edge. In the following, we describe the observed near-field amplitude and phase self-consistently using a simple cavity model formed between the PhP launching and scattering tip and propagating PhP reflecting the hBN crystal edge. As discussed in detail elsewhere, ${ }^{26}$ we model the complex-valued substrate response $\tilde{\Psi}$ from the dielectric sample response $\tilde{\psi}_{\mathrm{hBN}}$, the resonant local PhP response $\tilde{\psi}_{\mathrm{PhP}, 0}$, and the reflected PhP response $\tilde{\psi}_{\text {PhP, } 1}$ as $\tilde{\Psi}=\tilde{\psi}_{\mathrm{hBN}}+\tilde{\psi}_{\mathrm{PhP}, 0}+\tilde{\psi}_{\mathrm{PhP}, 1}$. To account for the spatial averaging by the tip, we convolve the sample response with a weighting function $\Theta$ to yield the modeled signal $\tilde{\mathrm{A}}(r)=\tilde{\Psi}\left(r^{\prime}\right) \times \Theta\left(r-r^{\prime}\right)$. To approximate the tip geometry, we use a Gaussian function for $\Theta$ with a width of 30 nm . We then fit the wavelength-dependent amplitude and phase simultaneously using this cavity model. Figure 4A and B show the experimental PhP response from 1380 to $1560 \mathrm{~cm}^{-1}$, and Figure 4 C and D show the corresponding results of the fit. Further shown in Figure 4 E and F are line cuts at select frequencies with the experimentally measured tip-edge distance dependencies of $|\mathrm{A}(\bar{\nu})|(\mathrm{E})$ and phase $\Phi(\bar{\nu})(\mathrm{F})$, in blue and red, respectively, and the fit results (black). From the fitting, we can estimate the polariton wavelength, reflection coefficients, and damping. We typically find a reflection coefficient of $R=-1$ (corresponding to a reflection phase of $\pi$ ) at the hBN edge. (The reflection coefficient and phase have large uncertainty due to the low polariton quality factor and the


Figure 5. Experimental (A) SINS amplitude $|A(\bar{\nu})|$ and (B) phase $\Phi(\bar{\nu})$ spatiospectral linescan in the region of the hBN out-of-plane phonon mode of the 147 nm thick hBN flake. Experimental amplitude (C) and phase (D) distance profiles extracted from (A) and (B), respectively. (E) Color map of the electrical field along the $c$-axis for the fundamental in-plane (top) and out-of-plane (bottom) phonon polariton modes.
uncertainty in defining the exact position of the hBN edge.) However, for the case of lower frequency PhP modes (1480, 1450, and $1420 \mathrm{~cm}^{-1}$ ) the increase in amplitude near the edge as seen in Figure 4 E suggests the possibility of a change in reflection coefficient. The bright amplitude response at $x=0$ may result from a change in the interaction geometry, whereby the tip interacts with the vertical edge of the flake, but could also be caused by the generation of PhPs at the edge itself. However, in contrast to the much stronger polarizability of the metallic tip, this edge contribution is expected to be weak and therefore neglected in our analysis. Further theoretical investigation will be required for a complete description of the PhP response and to fully understand the PhP reflection and its phase behavior at the hBN edges across the whole spectral range.

As noted above, hBN is a natural hyperbolic material, and in bulk hBN , many waveguide modes of phonon polaritons can exist. Their description requires the full knowledge of both the in-plane and out-of-plane dielectric constants. ${ }^{21,22}$ However, in the 2 D limit, where the hBN flake thickness can be a few tens of nanometers or even a few atomic layers, the only observable mode in our near-field microscopy study is the fundamental mode. All the other modes will have wavelengths shorter than or comparable to the film thickness because they require at least one full oscillation over the film thickness. The higher order polaritons, due to their very short wavelengths, are strongly confined in the bulk and do not couple efficiently to an external scattering center in the form of the tip in this case, and thus are not observed in our near-field experiment.

Similarly, the observed out-of-plane mode PhP response is weak (Figures 3,5) as compared to the higher frequency inplane mode PhP response (Figures 3, 4). Figure 5E is a schematic of the electrical field (along the $c$-axis or $z$-direction) distribution. The fundamental mode of in-plane PhP features the same sign of charge accumulated at the top and bottom surfaces of a thin BN flake, while the fundamental mode of the out-of-plane PhP features charge accumulation with opposite signs at the two surfaces. For the in-plane PhP mode, the electrical field is mainly outside the 2D material (Figure 5E, top panel); for the out-of-plane PhP mode, the electrical field is mainly concentrated inside the hBN flake. For ultrathin hBN flakes at the 2 D limit with $\lambda \gg d$, the polariton with opposite sign of charge at the top and bottom surfaces does not couple efficiently to the tip because the electrical field is strongly confined inside the 2D material. Therefore, the observed PhP feature for the out-of-plane mode is much weaker, and this effect becomes even stronger when the BN layer becomes thinner. Indeed, within our signal-to-noise ratio, we do not observe PhP features in the out-of-plane mode for thicknesses $d$ < 70 nm .

Besides the 160 nm thick and the 147 nm thick samples, we systematically measured a set of samples with thicknesses from 3 to 160 nm . Spatiospectral maps of near-field amplitude and phase at the in-plane phonon mode for three more samples with thicknesses of 7, 22, and 40 nm are displayed in Figure 6A and B . The gradual change of the in-plane PhP feature with sample thickness is clearly seen and is caused by the variation of polariton wavelength with hBN crystal thickness. Figure 6C shows the dependence of the polariton wavelengths $\lambda_{\mathrm{p}}$ on sample thickness $d$ for three selected frequencies at $\bar{\nu}=1410$, 1440 , and $1470 \mathrm{~cm}^{-1}$, exhibiting linear scaling behavior for all frequencies.

To understand the experimentally observed scaling behavior for the in-plane PhP mode, we present a general model describing 2 D polaritons in ultrathin materials where the thickness $d$ is much smaller than the polariton wavelength $\lambda_{\mathrm{p}}$. 2D polaritons are characterized by in-plane charge density oscillations, which generate an appreciable electrical field distribution near the surface that can couple efficiently to a tip via its near-field. The elementary charge oscillations can arise from free electrons, ions, and excitons, known respectively as plasmon, phonon, and exciton polaritons. In contrast, out-ofplane charge density oscillations generate a large electric field inside the 2 D material, but the field outside the material is negligible (at the level of $d / \lambda_{\mathrm{p}}$ ). Such out-of-plane modes, like the $780 \mathrm{~cm}^{-1}$ phonon in hBN, do not couple efficiently to a near-field probe and, thus, are less easily observed in our experiment.

For 2D polaritons associated with in-plane charge oscillations, the physics is uniquely determined by a single parameter the in-plane 2D susceptibility $\chi^{2 \mathrm{D}}=\chi_{\|}^{\text {bulk }} d=\left(\varepsilon_{\|}^{\text {bulk }}\right.$ $-1) d \square$ because the electrical field for the fundamental PhP mode in ultrathin hBN flakes is mainly in plane. Here $\chi_{\|}^{\text {bulk }}$ and $\varepsilon_{\|}^{\text {bulk }}$ are the in-plane bulk susceptibility and dielectric constant, respectively. The dispersion relation of 2D polaritons (in the long-wavelength limit) is then simply determined by a zero dynamical screening function $1+\varepsilon_{0}\left(q^{2} / e\right) \chi^{2 D}(\omega) \nu_{\mathrm{c}}^{2 \mathrm{D}}(q)=0,{ }^{31}$ where $\nu_{\mathrm{c}}^{2 \mathrm{D}}(q)=e /\left(2 \varepsilon_{0} \varepsilon_{\text {eff }} q\right)$ is the 2 D Coulomb interaction, $q=$ $2 \pi / \lambda_{\mathrm{p}}$ is the polariton wavevector, and $\varepsilon_{\text {eff }}$ is the effective dielectric constant due to the environmental screening. Consequently, we obtain a simple yet general solution for 2D polariton dispersion in ultrathin films of $\lambda_{\mathrm{p}}=-\left(\pi d / \varepsilon_{\text {eff }}\right)$ -


Figure 6. PhP dispersion and evolution of the in-plane phonon polariton wavelength with sample thickness. Spatiospectral maps of (A) SINS amplitude $|A(\bar{\nu})|$ and (B) phase $\Phi(\bar{\nu})$ for samples with thicknesses of 7, 22, and 40 nm . (C) Evolution of the in-plane phonon polariton wavelength, $\lambda_{p}$, with sample thickness, $d$, at three representative excitation frequencies: 1410,1440 , and $1470 \mathrm{~cm}^{-1}$ For thin hBN flakes, $\lambda_{\mathrm{p}}$ is proportional to sample thickness. (D) Experimental (colored curves) and theoretical (black curves) dispersion relations of in-plane PhPs on hBN flakes with different thicknesses. The horizontal dashed lines are the longitudinal $\left(\omega_{\mathrm{LO}}=\right.$ $1614 \mathrm{~cm}^{-1}$ ) and transverse ( $\omega_{\mathrm{TO}}=1370 \mathrm{~cm}^{-1}$ ) optical phonon frequencies of hBN.
$\left[\varepsilon_{\|}^{\text {bulk }}(\omega)-1\right]$. This simple model correctly predicts the linear scaling behavior between the phonon polariton wavelength $\lambda_{\mathrm{p}}$ and the thickness $d$ for a given frequency in thin hBN crystals (Figure 6C; here the value of the hBN dielectric function $\varepsilon_{\|}^{\text {buk }}(\omega)$ is from ref 11$)$. It also shows that a 2 D phonon polariton is independent of the perpendicular dielectric constant $\varepsilon_{\perp}^{\text {bulk }}(\omega)$ in thin crystals. Using an effective environmental dielectric constant $\varepsilon_{\text {eff }}=\left(\varepsilon_{\text {air }}+\varepsilon_{\mathrm{SiO}_{2}}\right) / 2$, our theory qualitatively reproduces the experimentally observed dispersion relation (Figure 6D). The deviation between theory and experimental data mainly originates from the inaccuracy of $\varepsilon_{\text {eff }}$ from neglecting the silicon substrate ( 300 nm away from the hBN layer) contribution, which is polariton wavelength dependent. The theoretical model is a good approximation only when the sample thickness is much smaller than the polariton wavelength. However, in addition to its application to PhPs in hBN, we expect this simple model to provide a good general description of any 2D polariton system, including plasmon polaritons in graphene, as well as phonon or exciton polaritons in other ultrathin crystals.

In summary, we have investigated phonon polaritons in hBN crystals of different thicknesses by using broadband synchro-
tron infrared near-field spectroscopy and imaging. We find that in the measured hBN basal plane a strong PhP response is observed only around the in-plane phonon mode, and the measured polariton wavelength is proportional to sample thickness. In contrast to the strong in-plane mode, the out-ofplane mode PhP response is weak. The observed scaling behavior for the in-plane phonon polariton mode can be well understood with a simple theory that is universal for polaritons in thin 2D materials. Our results open up new avenues in engineering infrared light at the nanometer scale for novel photonic nanodevices and understanding intriguing polariton behaviors in low-dimensional nanomaterials.

## METHODS

Approximately $500 \mu \mathrm{~W}$ of broadband synchrotron IR light from Beamline 5.4 at the Advanced Light Source (ALS) of Lawrence Berkeley National Laboratory is coupled to an asymmetric Michelson interferometer, consisting of a $50: 50 \mathrm{KBr} / \mathrm{Ge}$ beamsplitter (Thermo-Scientific), a modified commercial AFM (Innova, Veeco/Bruker), and a modified commercial FTIR spectrometer (Nicolet 6700, Thermo-Scientific). The beamsplitter directs half of the light to the scanning mirror in the FTIR spectrometer and directs the other half to a parabolic mirror (N.A. $\approx 0.4$ ) that focuses the beam onto a platinum silicide (PTSi-NCH, Nanosensors) AFM tip. The backscattered light from the AFM tip, collected by the same parabolic mirror, and the light reflected from the moving mirror are recombined on the beamsplitter and focused onto an MCT detector (KLD-$0.1-\mathrm{J} 1$, Kolmar). The AFM is operated in noncontact mode, and the tip-scattered signal is demodulated at twice the tiposcillation frequency (typically $250-300 \mathrm{kHz}$ ) with a lock-in amplifier (HF2Li-MF, Zurich Instruments). ${ }^{32,33}$ Spectra are acquired with interferometric heterodyne detection by moving the mirror in the modified FTIR spectrometer. ${ }^{25}$ The broad spectral range of the synchrotron source enables the acquisition of spectra across the entire mid-IR range ( $700-5000 \mathrm{~cm}^{-1}$ ) within a single scan. The Fourier transform of the resulting interferograms results in the complex-valued near-field spectrum. The real and imaginary spectra, typically represented as spectral amplitude and phase, relate to the complex dielectric function of the material. ${ }^{33,34}$

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## Author Contributions

Y.S. and Z.S. exfoliated the thin hBN samples. Z.S., H.A.B., Y.S., B.Z., and C.J. performed the near-field optical measurements. M.B.R., H.A.B., and M.C.M. developed SINS at the ALS. S.B. and M.B.R. developed the PhP near-field tip-boundary cavity model. H.A.B., Z.S., S.B., B.Z., H.C., and M.B.R. analyzed the data and made the figures. Z.S., H.A.B., F.W., S.B., and M.B.R. wrote the paper. F.W. developed the 2D polariton theory, conceived the experiment, and led the study. F.W., M.B.R., and M.C.M. supervised the project. All authors discussed the results.

## Author Contributions

${ }^{\mathrm{I}} \mathrm{Z}$. Shi and H. A. Bechtel contributed equally to this work.

## Notes

The authors declare no competing financial interest.

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